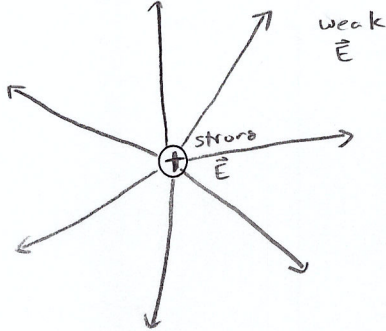
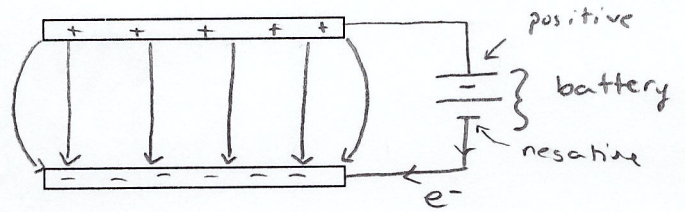


Electric Potential in a Uniform Field: Parallel Plates

- Compare the electric field around a point charge and the electric field between two parallel plates



use $\vec{E} = \frac{kq}{r^2}$
 b/c electric field strength depends on distance

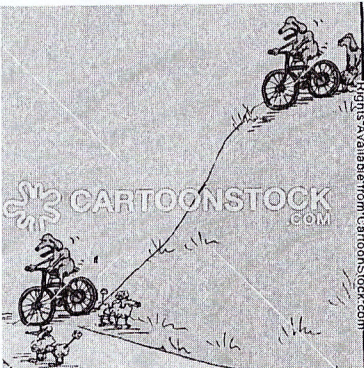


Uniform electric field
 b/w parallel plates

\therefore NEVER use $\vec{E} = \frac{kq}{r^2}$!

- * ○ Parallel plates are an example where the electric field strength is uniform
- We need a different equation to deal with this uniform electric field strength because so far our equations deal with a changing electric field strength
- To help us understand the equations used for a uniform electric field, you first need to understand the electric potential energy that occurs within the parallel plates
- Electric potential energy is very similar to gravitational potential energy
 - A charged object inside a uniform field can have high electric potential energy and low electric potential energy
 - The law of conservation of energy applies and electrical potential energy can be converted into kinetic energy and vice versa

Gravitational Potential Energy (E_p)

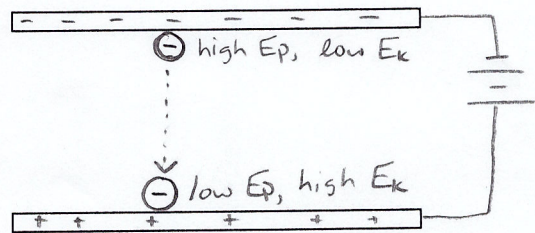


high E_p ,
 low E_k

low E_p ,
 high E_k

ΔE_p converted to ΔE_k

Electric Potential Energy (E_p)



ΔE_p converted to ΔE_k

* repulsion = high E_p
 attraction = low E_p

- Therefore uniform electric fields/parallel plates are a method to accelerated/decelerate charged particles.

- The change in the electric potential energy per unit charge is defined as the **electric potential difference** (or **electric potential** or **voltage**) and can be described by the following equation:

$$\Delta V = \frac{\Delta E}{q}$$

where ΔV is potential difference in units of volts (V)

ΔE is the change in energy in joules (J)

q is charge in coulombs (C)

* not electric field (\vec{E})

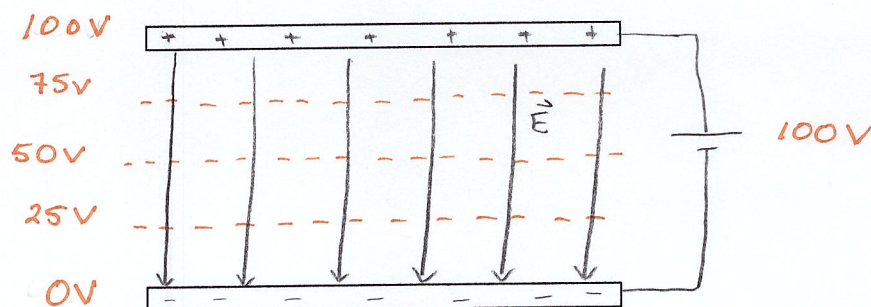
- Potential difference is a scalar quantity
- Small amounts of energy can also be measured in units of **electron volts (eV)**. However, joules are the SI units for energy, so all calculations involving energy in formulas need to be done in joules!

$$1 \text{ eV} = 1.6 \times 10^{-19} \text{ J} \quad \text{on data sheet!}$$

EXAMPLE: Convert 2.10 eV into joules.

$$2.10 \text{ eV} \times \left(\frac{1.6 \times 10^{-19} \text{ J}}{1 \text{ eV}} \right) = \boxed{3.36 \times 10^{-19} \text{ J}}$$

- * • Since the electric potential energy is changing between a set of parallel plates based on electrostatic repulsion/attraction, the electric potential is also changing, even though the electric field remains uniform



- Even though the electric field between a set of parallel plates is uniform, the electric field strength can be altered by either changing the separation distance of the plates or the electric potential between the plates as shown by the following equation:

$$\vec{E} = \frac{\Delta V}{d}$$

where \vec{E} is electric field strength (N/C or V/m)
 ΔV is potential difference between plates (V)
 d is distance between plates (m)

EXAMPLES:

1. An electric field of 3000V/cm may cause the air to ionize and allow electrons to jump from one surface to another causing a spark. An electrostatic charge is produced on a student walking across a rugged floor. He reaches for a doorknob. Assuming an electric field of 3000V/cm, determine the electric potential difference required between the finger and doorknob to produce a spark when they are separated by 1.2cm.

$$\vec{E} = 3000 \text{ V/cm}$$

$$d = 1.2 \text{ cm}$$

$$\Delta V = ?$$

$$\vec{E} = \frac{\Delta V}{d} \Rightarrow \vec{E} d = \Delta V$$

$$\Delta V = (3000 \text{ V/cm})(1.2 \text{ cm}) = 3600 \text{ V}$$

$$\boxed{\Delta V = 3.6 \times 10^3 \text{ V}}$$

$$q = 1.6 \times 10^{-19} \text{ C}$$

$$m = 9.11 \times 10^{-31} \text{ kg} \quad \text{from data sheet!}$$

2. An electron has a speed of $5.80 \times 10^5 \text{ m/s}$ when it enters a set of parallel plates. If the electric potential difference between the plates is 140 V , what is the exit speed of the electron?

$$v_i = 5.80 \times 10^5 \text{ m/s}$$

$$\Delta V = 140 \text{ V}$$

$$v_f = ?$$

$$\textcircled{2} \begin{cases} E_k = \frac{1}{2} m v^2 \\ \downarrow \\ \Delta E_k = E_{kf} - E_{ki} \end{cases}$$

$$\textcircled{1} \Delta V = \Delta E / q$$

$$\textcircled{1} \Delta E = \Delta V q = (140 \text{ V})(1.6 \times 10^{-19} \text{ C}) = 2.24 \times 10^{-17} \text{ J}$$

$$\textcircled{2} \Delta E = E_{kf} - E_{ki} \Rightarrow E_{kf} = \Delta E + E_{ki} = \Delta E + \frac{1}{2} m (v_i)^2$$

$$E_{kf} = 2.24 \times 10^{-17} \text{ J} + \frac{1}{2} (9.11 \times 10^{-31} \text{ kg})(5.80 \times 10^5 \text{ m/s})^2$$

$$E_{kf} = 2.24 \times 10^{-17} \text{ J} + 1.532302 \times 10^{-17} \text{ J}$$

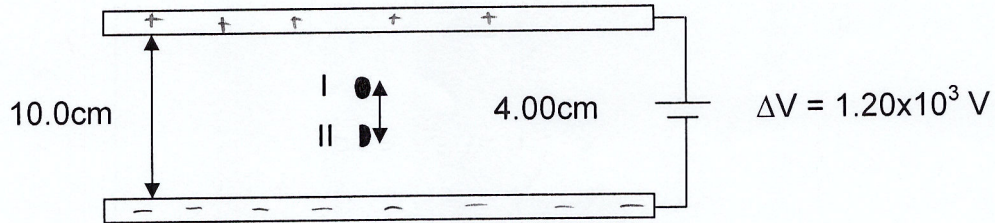
$$E_{kf} = 2.255 \dots \times 10^{-17} \text{ J}$$

$$E_{kf} = \frac{1}{2} m (v_f)^2 \Rightarrow v_f = \sqrt{\frac{2E_k}{m}}$$

$$v_f = \sqrt{\frac{2(2.255 \dots \times 10^{-17} \text{ J})}{9.11 \times 10^{-31} \text{ kg}}} = 7.0365 \dots \times 10^6 \text{ m/s}$$

$$v_f = 7.04 \times 10^6 \text{ m/s}$$

- * 3. The diagram below shows two parallel plates separated by 10.0cm. Calculate the change in voltage between points I and II when they are 4.00cm apart.



uniform \vec{E} , but changing ΔV !

B/w Plates

$$\Delta V_1 = 1.20 \times 10^3 \text{ V}$$

$$d_1 = 0.100 \text{ m}$$

within Plates

$$\Delta V_2 = ?$$

$$d_2 = 0.0400 \text{ m}$$

$$\textcircled{1} \quad \vec{E} = \frac{\Delta V_1}{d_1}$$

B/w plates

$$\vec{E} = \frac{\Delta V_2}{d_2} \text{ within plates} \quad \textcircled{2}$$

$$\textcircled{1} \quad \vec{E} = \frac{\Delta V_1}{d_1} = \frac{1.20 \times 10^3 \text{ V}}{0.100 \text{ m}} = 12000 \text{ N/C}$$

$$\textcircled{2} \quad \vec{E} = \frac{\Delta V_2}{d_2} \Rightarrow \Delta V_2 = \vec{E} d_2$$

$$\Delta V_2 = (12000 \text{ N/C})(0.0400 \text{ m}) = 480 \text{ V}$$

$$\Delta V_2 = 480 \text{ V}$$

Practice Problems

1. A cell membrane is $1.0 \times 10^{-7} \text{ m}$ thick and has an electric potential difference between its surfaces of 0.070 V . What is the electric field within the membrane?
[$7.0 \times 10^5 \text{ V/m}$]
2. How much electrical potential energy (in eV) does an alpha particle gain when it moves between two oppositely charged parallel plates with a voltage of 20000 V ?
[$4.00 \times 10^4 \text{ eV}$]
3. An electron starts from rest and accelerates across two parallel plates to obtain a kinetic energy of $9.6 \times 10^{-17} \text{ J}$.
 - a. Determine the potential difference between the plates. **[600 V]**
 - b. Determine the electric potential energy the electron initially possessed.
[$9.6 \times 10^{-17} \text{ J}$]
 - c. Determine the maximum speed of the electron. **[$1.45 \times 10^7 \text{ m/s}$]**
4. What potential difference is needed to decelerate an alpha particle from $1.40 \times 10^6 \text{ m/s}$ to $6.80 \times 10^5 \text{ m/s}$. **[$1.56 \times 10^4 \text{ V}$]**
5. Two parallel plates are separated by a distance of 3.75 cm . Two points, A and B, lie along a perpendicular line between the parallel plates and are 1.10 cm apart. Between the two points, there is a difference in electric potential of 6.00 V . Calculate the electric potential between the parallel plates. **[20.5 V]**
6. The cell membrane may be thought of as a set of charged parallel plates. The electric potential difference between the outside and the inside of the membrane is about 0.70 V and the thickness of the membrane is $5.0 \times 10^{-9} \text{ m}$. If 0.18 eV is used to move a Na^+ ion (has $+1$ elementary charge), how far does the Na^+ move across the membrane? **[$1.3 \times 10^{-9} \text{ m}$]**

Show that a $\frac{N}{c} = \frac{V}{m}$

$$\frac{\cancel{J}}{m} \times \left(\frac{J/c}{\cancel{J}} \right) = \frac{\cancel{J}}{m \cdot c} \times \left(\frac{kg \cdot m^2/s^2}{\cancel{J}} \right) = \frac{kg \cdot m^2/s^2}{m \cdot c}$$

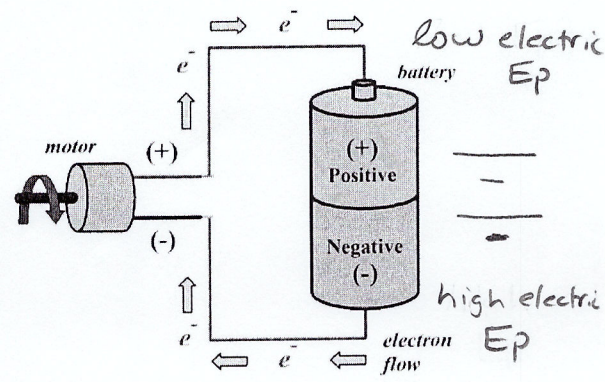
$$= \frac{kg \cdot m/s^2}{c}$$

but $F=ma \therefore \frac{kg \cdot m/s^2}{c} \times \left(\frac{N}{kg \cdot m/s^2} \right)$

$$= \frac{N}{c}$$

$\rightarrow \Delta V$

- A battery is a source of potential difference
 - Just as a water pump can increase the gravitational potential energy of water, a battery will increase the electrical potential energy of a charge
 - * ○ Electric potential is the "pushing power" behind charges; pushing charges to a higher electric potential energy



- When a potential difference is applied to a circuit, a current is created. **Current (I)** is the flow rate of electric charge
 - EXAMPLE: A battery is a voltage source that causes a current to flow through a mp3 player and produces the music you hear
 - The definition of current is also expressed as an equation

$$I = q/t$$

where I is current (C/s or A)
 q is charge (C) total charge!
 t is time (s)

- **Ampere (amps or A):** fundamental unit of current

if 5000 electrons passed through a wire in 9.25s, what is the current?

$$I = \frac{q}{t} = \frac{5000 \times 1.6 \times 10^{-19} \text{ C}}{9.25 \text{ s}} = 9.2 \times 10^{-17} \text{ A}$$

$I = 9.2 \times 10^{-17} \text{ A}$

4. A cell phone charger runs on a current of 900mA. How many electrons pass through a charging cell phone if the cell phone is only plugged in the charger for 15.0 minutes?

$$I = 900 \text{ mA} \times \left(\frac{10^{-3} \text{ A}}{\text{mA}} \right) = 0.900 \text{ A}$$

$$t = 15.0 \text{ min.} \times \left(\frac{60 \text{ s}}{1 \text{ min}} \right) = 900 \text{ s}$$

$$\# \text{ electrons} = \frac{q_{\text{total}} \text{ (2)}}{q_{e^-}} \rightarrow I = \frac{q_{\text{total}} \text{ (1)}}{t}$$

$$\text{(1)} \quad I = \frac{q_{\text{total}}}{t} \rightarrow q_{\text{total}} = It = (0.900 \text{ A})(900 \text{ s})$$
$$q_{\text{total}} = 810 \text{ C}$$

$$\text{(2)} \quad \# \text{ electrons} = \frac{810 \text{ C}}{1.60 \times 10^{-19} \text{ C}} = 5.0625 \times 10^{21} \text{ electrons}$$

$$\# \text{ electrons} = 5.06 \times 10^{21} \text{ electrons}$$

$$q = +1e = +1.60 \times 10^{-19} \text{ C}$$

$$\uparrow \rightarrow m = 1.67 \times 10^{-27} \text{ kg}$$

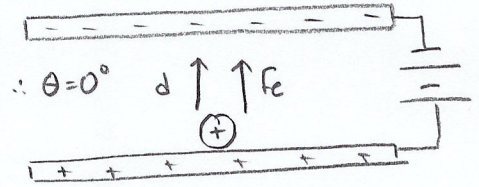
5. A proton is placed in an electric field between two parallel plates. If the plates are 6.0 cm apart and have a potential difference between them of 75 V, how much work is done against the electric field when the proton is moved 3.0 cm parallel to the electric field?

$$d_{\text{plates}} = 6.0 \text{ cm} \times \left(\frac{10^{-2} \text{ m}}{1 \text{ cm}} \right) = 0.060 \text{ m}$$

$$\Delta V = 75 \text{ V}$$

$$W = ?$$

$$d_{\text{particle}} = 3.0 \text{ cm} = 0.030 \text{ m}$$



$$\textcircled{2} \quad W = \Delta E = F d_{\text{particle}} \cos \theta \quad \cos(0^\circ) = 1$$

* could use either
or!
(energy or
forces)!

$$\vec{E} = \frac{\vec{F}_e}{q} \quad \textcircled{2}$$

$$\vec{E} = \frac{\Delta V}{d_{\text{plates}}} \quad \textcircled{1}$$

$$\textcircled{1} \quad \vec{E} = \frac{\Delta V}{d_{\text{plates}}} = \frac{75 \text{ V}}{0.060 \text{ m}} = 1250 \text{ V/m}$$

$$\textcircled{2} \quad \vec{E} = \frac{\vec{F}_e}{q} \rightarrow \vec{F}_e = \vec{E} q = (1250 \text{ V/m})(1.60 \times 10^{-19} \text{ C})$$

$$\vec{F}_e = 2.0 \times 10^{-16} \text{ N}$$

$$\textcircled{3} \quad W = F d_{\text{particle}} = (2.0 \times 10^{-16} \text{ N})(0.030 \text{ m})$$

$$W = 6.0 \times 10^{-18} \text{ J}$$

$$\text{OR} \quad 6.0 \times 10^{-18} \text{ J} \times \left(\frac{1 \text{ eV}}{1.60 \times 10^{-19} \text{ J}} \right) = 38 \text{ eV}$$

Now try pg. 108 # 6, 7 & pg. 115 #30, 33 & Practice Problem

↑
current

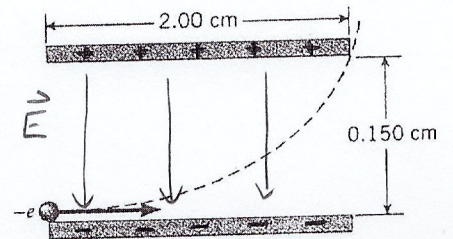
force

Practice Problem

1. An alpha particle travelling at a uniform speed of 4.50×10^3 m/s enters an electric field of 250 N/C between two charged plates separated by 10.0cm. Determine the speed of the alpha particle when it reaches the far plate if it entered through a hole in the positive plate. [**4.93×10^4 m/s**]

- * In the previous examples, we only considered problems where the charged particles are moving parallel to the field. Therefore, if force and distance are parallel to each other, work is being done and the particles accelerate.
 - o Recall though that if a particle is moving perpendicular to the force, no work is being done and therefore the particles maintain uniform motion

EXAMPLE: The drawing shows an electron entering the lower left side of two parallel plates and exiting at the upper right side. The initial speed of the electron is 7.00×10^6 m/s. The parallel plates are 2.00 cm long and separated by 0.150 cm. Calculate the electric field strength inside the parallel plates.



* Similar to projectile motion *

Horizontal / Perpendicular
(uniform motion)

$$v = \frac{d}{t}$$

$$v = 7.00 \times 10^6 \text{ m/s}$$

$$d = 0.02 \text{ m}$$

$$t =$$

Vertical / Parallel
(accelerated)

$$d = 0.0015 \text{ m}$$

$$v_i = 0.0 \text{ m/s}$$

$$t =$$

$$a = ?$$

$$\textcircled{2} d = \cancel{v_i t} + \frac{1}{2} a t^2$$

$$\frac{2d}{t^2} = a = \frac{(2)(0.0015 \text{ m})}{(2.857 \dots \times 10^{-9} \text{ s})^2} = 3.675 \times 10^{14} \text{ m/s}^2$$

$$\textcircled{1} v = \frac{d}{t} \Rightarrow t = \frac{d}{v}$$

$$t = \frac{0.02 \text{ m}}{7.00 \times 10^6 \text{ m/s}}$$

$$t = 2.857 \dots \times 10^{-9} \text{ s}$$

$$\textcircled{3} F_{\text{net}} = ma = F_e + (-F_g)$$

o * negligible for atomic particles

$$\therefore F = ma = (9.11 \times 10^{-31} \text{ kg})(3.675 \times 10^{14} \text{ m/s}^2)$$

$$F_e = 3.3479 \dots \times 10^{-16} \text{ N}$$

$$\textcircled{4} \vec{E} = \frac{F_e}{q} = \frac{(3.3479 \dots \times 10^{-16} \text{ N})}{1.6 \times 10^{-19} \text{ C}} = 2.092 \dots \times 10^3 \text{ N/C}$$

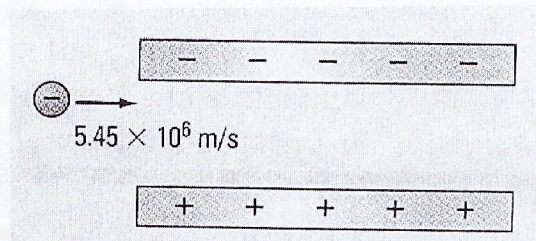
$$\therefore \boxed{\vec{E} = 2.09 \times 10^3 \text{ N/C, down}}$$

Now try pg. 115 # 31-32 and Practice Problems

Practice Problems

1. An electron, travelling at $2.3 \times 10^3 \text{ m/s}$, enters perpendicular to the electric field between two horizontal charged parallel plates. If the electric field strength is $1.5 \times 10^2 \text{ V/m}$, calculate the time taken for the electron to deflect a distance of $1.0 \times 10^{-2} \text{ m}$ toward the positive plate. **$[2.8 \times 10^{-8} \text{ s}]$**

2. An electron, travelling horizontally at a speed of $5.45 \times 10^6 \text{ m/s}$, enters a parallel plate capacitor with an electric field of 125 N/C between the plates, as shown in the figure.



- Sketch the electric field lines between the plates and the motion of the electron through the capacitor.
 - Calculate the acceleration of the electron. **$[2.20 \times 10^{13} \text{ m/s}^2, \text{ down}]$**
 - If the electron falls a vertical distance of $6.20 \times 10^{-3} \text{ m}$ toward the positive plate, how far will the electron travel horizontally between the plates? **$[0.130 \text{ m}]$**
3. A proton is fired parallel in between a set of parallel plates at a height that is exactly midway between the set of plates with an initial speed of $2.50 \times 10^6 \text{ m/s}$, as shown in the diagram below. The electric potential difference between the plates is 175 V . If the proton travelled a total distance of 15.0 cm parallel to the plates, what is the separation distance between the plates? **$[0.777 \text{ cm}]$**

